

# Question 7

**Q:** How to input the parameters of anisotropic materials?

**A:** Please refer to the next slides.

- Piezoelectric material is anisotropic. Input elastic and piezoelectric properties, and permittivity in the form of a matrix.
- Be aware that the suffix for the compliance matrix may be represented as S, and the suffix for the stiffness matrix may be represented as C in the material supplier's data sheets. This is due to their technological background.
- The matrix has a symmetry. The elements only in the lower triangular matrix are required for setting material properties. The elements in gray on the right diagram are not required.
- Material data sheets may not always list all the values of elements. Required properties may need to be calculated using some laws with respect to those properties.
- Femtet may already specify the default value of 0 to some elements. The value other than 0 is special.

**Elasticity (Compliance) Matrix**

S11					
S21	S22				
S31	S32	S33			
0.0	0.0	0.0	S44		
0.0	0.0	0.0	0.0	S55	
0.0	0.0	0.0	0.0	0.0	S66


**Piezoelectricity Matrix**

0.0	0.0	0.0	0.0	d15	0.0
0.0	0.0	0.0	d24	0.0	0.0
d31	d32	d33	0.0	0.0	0.0

**Relative Permittivity Matrix**

$\epsilon_{11}$		
0.0	$\epsilon_{22}$	
0.0	0.0	C33

\*In the event of quartz or other single crystals, a value other than 0 may be specified to an element that would have a default value of 0.

## Example: Piezoelectric Ceramic (Hexagonal Crystal) d-Form

- The input locations in a matrix differ due to the varying symmetry of material properties based on the type of piezoelectric material or crystal system.
- The relations below are known when d-form is used for piezoelectric ceramics.

$$S_{22}=S_{11}$$

$$S_{32}=S_{31}$$

$$S_{55}=S_{44}$$

$$d_{32}=d_{31}$$

$$d_{24}=d_{15}$$

$$\epsilon_{22}=\epsilon_{11}$$

Elasticity (Compliance) Matrix ( $S^E$ )

S11					
S21	S11				
S31	S31	S33			
0.0	0.0	0.0	S44		
0.0	0.0	0.0	0.0	S44	
0.0	0.0	0.0	0.0	0.0	S66


Piezoelectricity Matrix ( $d$ )

0.0	0.0	0.0	0.0	d15	0.0
0.0	0.0	0.0	d15	0.0	0.0
d31	d31	d33	0.0	0.0	0.0

Relative Permittivity Matrix ( $\epsilon^T$ )

$\epsilon_{11}$		
0.0	$\epsilon_{22}$	
0.0	0.0	C33

## Example: Quartz (Trigonal Crystal) e-Form

- The input locations in a matrix differ due to the varying symmetry of material properties based on the type of piezoelectric material or crystal system.

- The relations below are known when e-form is used for quartz.

$$C_{22}=C_{11}$$

$$C_{32}=C_{31}$$

$$C_{55}=C_{44}$$

$$C_{42}=-C_{41}$$

$$C_{65}=C_{41}$$

$$C_{66}=0.5*(C_{11}-C_{12})$$

$$e_{12}=-e_{11}$$

$$e_{25}=-e_{14}$$

$$e_{26}=-e_{11}$$

$$\epsilon_{22}=\epsilon_{11}$$

Elasticity (Stiffness) Matrix ( $C^E$ )

C11					
C21	C11				
C31	C31	C33			
C41	-C41	0.0	C44		
0.0	0.0	0.0	0.0	C44	
0.0	0.0	0.0	0.0	C41	C66


Piezoelectricity Matrix ( $e$ )

d11	-d11	0.0	d14	0.0	0.0
0.0	0.0	0.0	0.0	-d14	-d11
0.0	0.0	0.0	0.0	0.0	0.0

Relative Permittivity Matrix ( $\epsilon^S$ )

$\epsilon_{11}$		
0.0	$\epsilon_{22}$	
0.0	0.0	C33